

# Preparation of XAFS Samples

Grant Bunker  
Professor of Physics  
BCPS Department/CSRRI  
Illinois Institute of Technology

# Acknowledgements

- Ed Stern, Dale Sayers, Farrel Lytle, Steve Heald, Tim Elam, Bruce Bunker and other members of the UW XAFS group
- Firouzeh Tannazi (IIT/BCPS) (results on fluorescence in complex materials)
- Suggested References:
  - Steve Heald's article "designing an EXAFS experiment" in Koningsberger and Prins and early work cited therein
  - Rob Scarrow's notes posted at [http://cars9.uchicago.edu/xafs/NSLS\\_2002/](http://cars9.uchicago.edu/xafs/NSLS_2002/)
  - *New book, "Introduction to XAFS", in press 2009, G. Bunker, Cambridge University Press*

# Sample prep - so what?

- If you want to get correct answers with XAFS, you have to pay attention to a few things at the very beginning.
- Even nowadays the literature is rife with data that suffer from unrecognized problems that should have been avoided.
- It's much easier to prevent the problems than to try to fix them afterward. Especially when you find out your thesis data is broken.

# types of samples

- solids
  - powders
  - heterogeneous collections of particles
  - films
  - lumps
- solutions
- gases
- XAFS vs temperature, pressure, pH, applied fields ...

# Safety issues

- Before preparing samples, check the MSDS's for the materials you are using.
- Most samples must be encapsulated in a manner that is consistent with their physical form and degree of hazard.

# Experimental Modes

- Modes:
  - Transmission
  - Fluorescence
  - Electron yield
- Designing the experiment requires an understanding of sample preparation methods, experimental modes, and data analysis

# Transmission

- Simplest XAFS measurement
- Measure relative x-ray flux transmitted through homogeneous sample

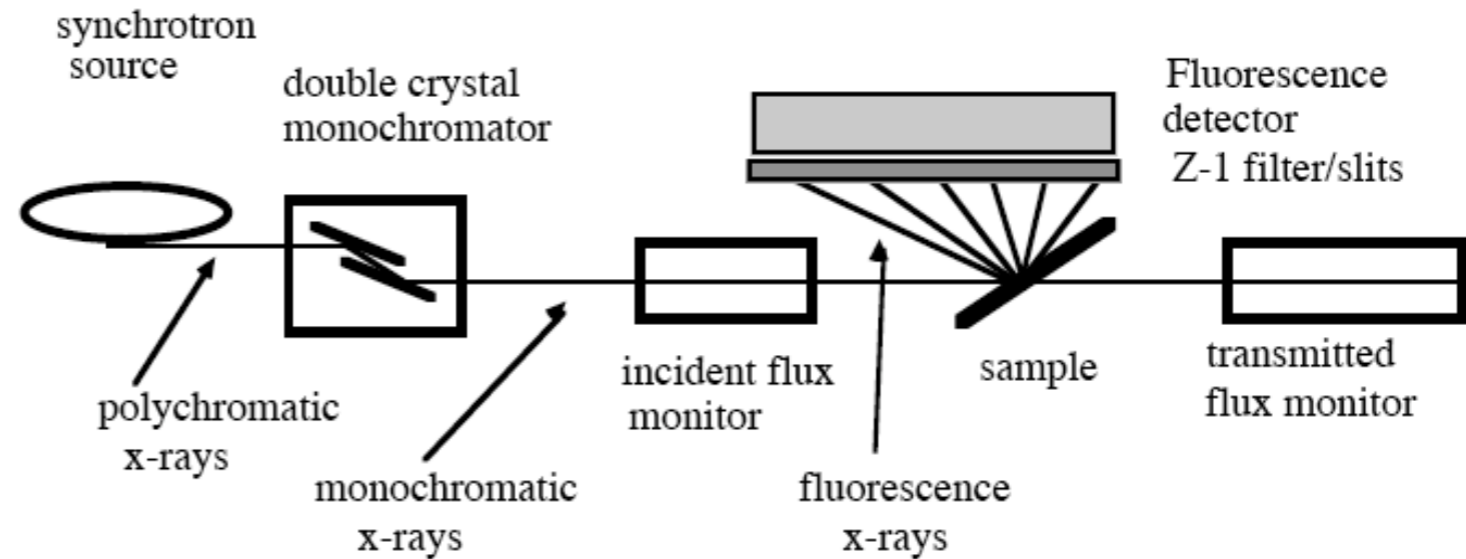


Figure 1 – Schematic XAFS experiment

# which mode to use?

- If you can readily get x-rays through the sample + substrate (and the edge step is  $> 0.1$ ), use transmission, otherwise use fluorescence or electron yield.
- If the sample is dilute, use fluorescence. If it is not dilute, the data may be distorted and fluorescence corrections may be needed. Alternatively use electron yield detection.
- Even if the sample is dilute on average, you have to deal with particle size issues.
- more on this later ...



# potential pitfalls

- thickness effects in transmission
- fluorescence self-absorption
- particle size

# transmission: uniform sample

Uniform, homogeneous sample:

$$\frac{I}{I_0} = \exp(-\mu(E)x)$$

$x$  is the sample thickness

$\mu(E)$  is the linear x-ray absorption coefficient  
at x-ray energy  $E$

Decreases roughly as  $1/E^3$  between absorption edges

# Absorption Length

$$\text{"Absorption Length"} \equiv 1/\mu$$

- It is the distance over which x-ray intensity decreases by factor  $1/e \sim 37\%$
- *Determines the basic length scale for choosing sample thickness, particle size, and sample homogeneity*
- *Determine its value at the energy of interest when designing experiments*

# Absorption Coefficient

Single substance:

$$\mu = \rho\sigma$$

$\rho$  is the density;  $\sigma$  is the cross section.

If the units of  $\rho$  are  $\text{g}/\text{cm}^3$  the cross section is in  $\text{cm}^2/\text{g}$ .

If the units of  $\rho$  are  $\text{atoms}/\text{cm}^3$  the cross section is in  $\text{cm}^2/\text{atom}$ .

$$1\text{barn} = 10^{-24}\text{cm}^2.$$

# Cross section

Interaction between a beam of particles  
(photons) and a target

Definition of "cross section"  $\sigma$ :

$$R\left[\frac{\text{photons}}{\text{s}}\right] = \Phi\left[\frac{\text{photons}}{\text{s} * \text{cm}^2}\right] * \sigma\left[\frac{\text{cm}^2}{\text{atom}}\right] * N[\text{atom}],$$

alternatively

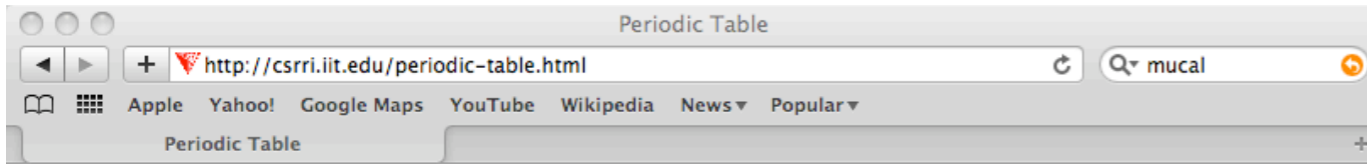
$$R\left[\frac{\text{photons}}{\text{s}}\right] = \Phi\left[\frac{\text{photons}}{\text{s} * \text{cm}^2}\right] * \sigma\left[\frac{\text{cm}^2}{\text{g}}\right] * M[\text{g}]$$

If the atomic cross section is on a per-mass basis,  
it is often called the "linear mass attenuation coefficient".

# Sources of Cross Section Data

- W.H. McMaster et al. Compilation of X-ray Cross Sections. Lawrence Radiation Laboratory Report UCRL-50174, National Bureau of Standards, pub. (1969).  
<http://www.csrri.iit.edu/mucal.html>  
<http://www.csrri.iit.edu/periodic-table.html>
- J.H. Hubbell, Photon Mass Attenuation and Energy-Absorption Coefficients from 1 keV to 20 MeV, Int. J. Appl. Radiat. Isot. 33, 1269-1290 (1982)
- S. Brennan and P.L. Cowan, Rev. Sci. Instrum, vol 63, p.850 (1992).
- B. L. Henke, E. M. Gullikson, and J. C. Davis, Atomic Data and Nuclear Data Tables Vol. 54 No. 2 (1993).  
[http://www-cxro.lbl.gov/optical\\_constants/atten2.html](http://www-cxro.lbl.gov/optical_constants/atten2.html)  
[http://www-cxro.lbl.gov/optical\\_constants/](http://www-cxro.lbl.gov/optical_constants/)
- C. T. Chantler, J. Phys. Chem. Ref. Data 24, 71 (1995)  
<http://physics.nist.gov/PhysRefData/FFast/html/form.html>
- W.T. Elam, B.Ravel, and J.R. Sieber, Radiat. Phys. Chem. v.63 (2002) pp 121-128.

# mucal - online cross sections for elements



## Periodic Table

Click on any button with element name to get its x-ray properties. If you give an energy value in the box at the top of the table then you also get x-ray cross-sections at that energy. The original subroutine (mucal.f or mucal.c) used to calculate x-ray cross-sections is available from [here](#).

Energy:  keV - Please note that values above 500 will be treated as eV rather than keV

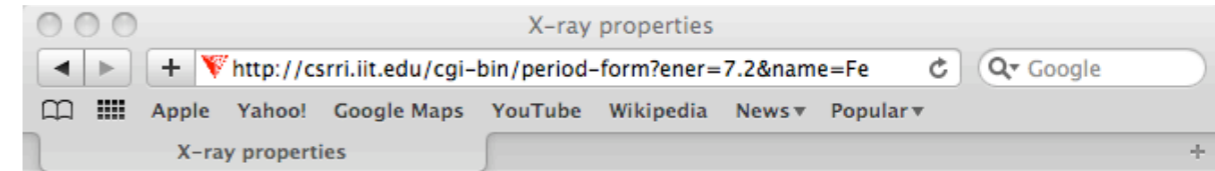
1 H																	2 He
3 Li	4 Be											5 B	6 C	7 N	8 O	9 F	10 Ne
11 Na	12 Mg											13 Al	14 Si	15 P	16 S	17 Cl	18 Ar
19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr
37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe
55 Cs	56 Ba	71 Lu	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn
87 Fr	88 Ra	103 Lr	104 Rf	105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Ds	111 Rg	112 Uub	113 Uut	114 Uuq	115 Uup	116 Uuh		
Lanthanide series																	
		57 La	58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb		
Actinide series																	
		89 Ac	90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No		

Created by Pathikrit Bandyopadhyay, recent updates by Carlo Segre.

Calculations are based on data compiled by **W. H. McMaster et. al.** Compilation of X-ray Cross-Sections, National Bureau of Standards, for calculation of x-ray cross sections.

Fluorescence yield data by **M. O. Krause** J. Phys. Chem. Ref. Data. 8, 307(1979)

Please report problems to [Carlo Segre \(segre@iit.edu\)](mailto:segre@iit.edu).



## X-ray properties

Element		Edge Energies (keV)		Edge jumps		Fluorescence yield	
Symbol	Fe	K	7.11199999	K	8.0714798	K	0.34000004
Z	26	L1	0.842000008	L1	1.1567719	L1	0.0010000005
Atomic Weight	55.8499985	L2	0.719900012	L2	NAN	L2	0.00630000001
Density	7.86000013	L3	0.706799984	L3	0.	L3	0.00630000001
		M	0.0939999968				
		K-alpha	6.40299988				
		K-beta	7.05700016				
		L-alpha	0.				
		L-beta	0.				

Cross-sections at E = 7.19999981 keV (cm <sup>2</sup> /gm)	
Photoelectric	393.506775
Coherent	1.797014
Incoherent	0.0686381012
Total	395.372406
Conversion factor (C) {(Barns/Atom) = C * (cm <sup>2</sup> /gm)}	92.7399979
Absorption coefficient	3107.6272 1/cm
1/mu (element)	3.21788907 microns

Created by Pathikrit Bandyopadhyay, recent updates by Carlo Segre.

Calculations are based on data compiled By **W. H. McMaster et. al.**

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# compounds

Absorption coefficient approximately given by

$$\mu \approx \sum_i \rho_i \sigma_i = \rho_M \sum_i \frac{m_i}{M} \sigma_i = \rho_N \sum_i \frac{n_i}{N} \sigma_i$$

where  $\rho_M$  is the mass density of the material as a whole,  $\rho_N$  is the number density of the material as a whole, and  $m_i/M$  and  $n_i/N$  are the mass fraction and number fraction of element  $i$ .



# Example Calculation

Fe<sub>3</sub>O<sub>4</sub> (magnetite) at 7.2 KeV;

<http://www.csrri.iit.edu/periodic-table.html>

density  $5.2 \frac{\text{g}}{\text{cm}^3}$

$$\text{MW} = 3 * 55.9 \frac{\text{g}}{\text{mol}} + 4 * 16.0 \frac{\text{g}}{\text{mol}} = 231.7 \frac{\text{g}}{\text{mol}}$$

$$\sigma_{\text{Fe}} = 393.5 \frac{\text{cm}^2}{\text{g}}; M_{\text{Fe}} = 55.9 \frac{\text{g}}{\text{mol}};$$

$$f_{\text{Fe}} = 55.9 / 231.7 = .724;$$

$$\sigma_{\text{O}} = 15.0 \frac{\text{cm}^2}{\text{g}}; M_{\text{O}} = 16.0 \frac{\text{g}}{\text{mol}};$$

$$f_{\text{O}} = 16.0 / 231.7 = .276;$$

$$\begin{aligned} \mu &= 5.2 \frac{\text{g}}{\text{cm}^3} (.724 * 393.5 \frac{\text{cm}^2}{\text{g}} + .276 * 15.0 \frac{\text{cm}^2}{\text{g}}) \\ &= 1503 / \text{cm} = .15 / \text{micron} \end{aligned}$$

$$\text{Absorption Length} = 1 \mu\text{m} / .15 = 6.7 \text{ microns}$$

Even if you don't know the density exactly, you can estimate it from something similar. It's probably between 2 and 8 g/cm<sup>3</sup>

# Transmission: nonuniform sample

What's the  
problem with  
nonuniform  
samples?

Characterized by thickness distribution  $P(x)$

$$\mu x_{\text{eff}}(E) = -\ln \int_0^{\infty} P(x) \exp(-\mu(E)x) dx$$

$$= -\sum_{n=1}^{\infty} \frac{C_n (-\mu)^n}{n!},$$

where  $C_n$  are the cumulants of the thickness distribution ( $C_1 = \bar{x}$ ,  $C_2 =$  mean square width, etc.)

A Gaussian distribution of width  $\sigma$  has

$$\mu x_{\text{eff}}(E) = \mu \bar{x} - \mu^2 \sigma^2 / 2$$

ref gb dissertation 1984

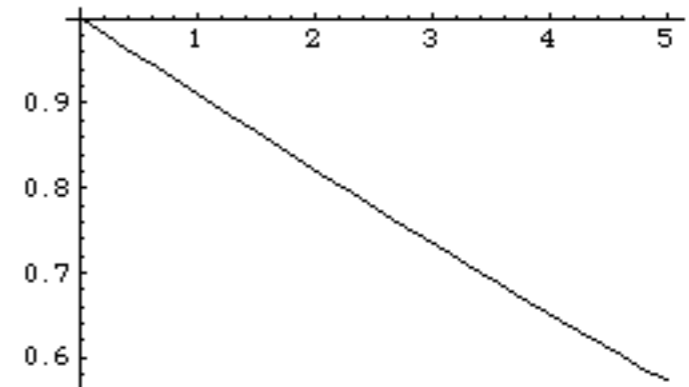
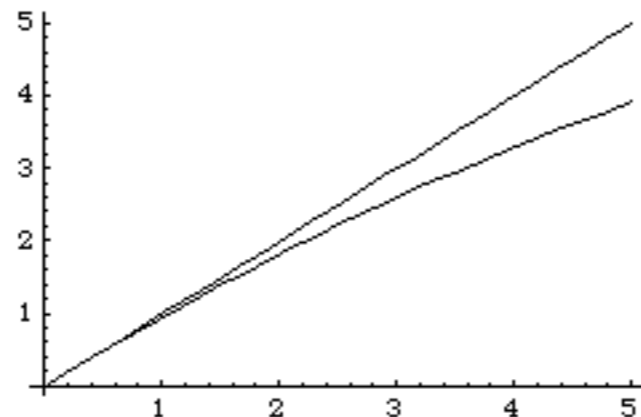
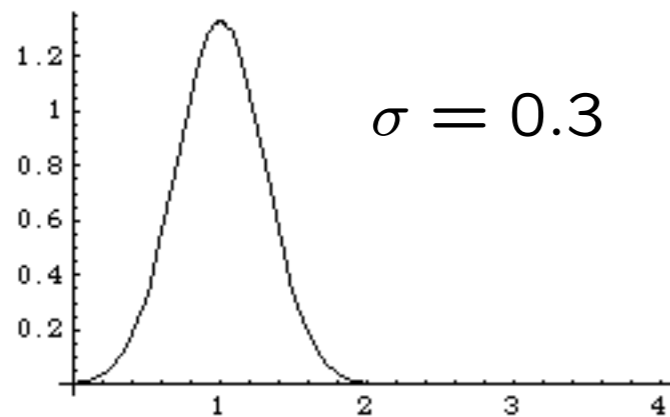
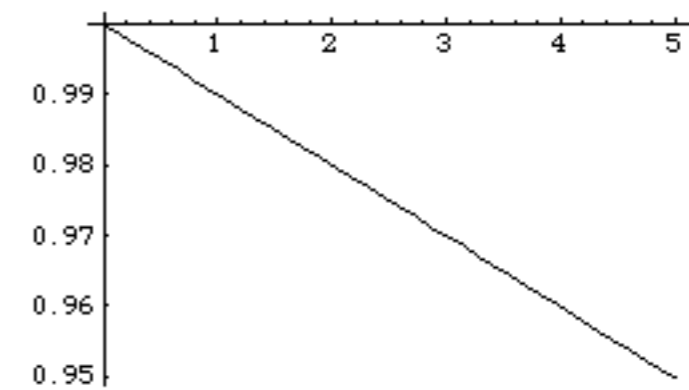
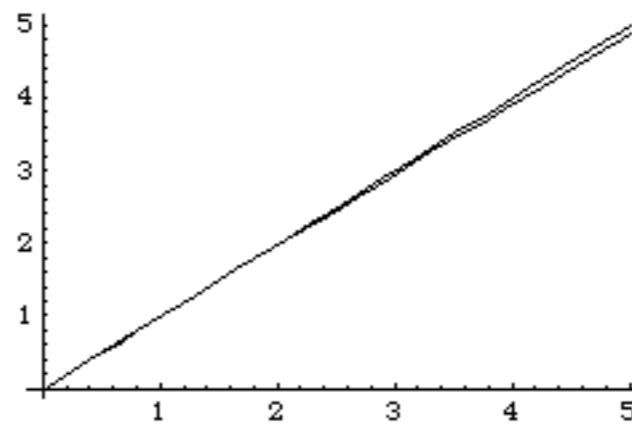
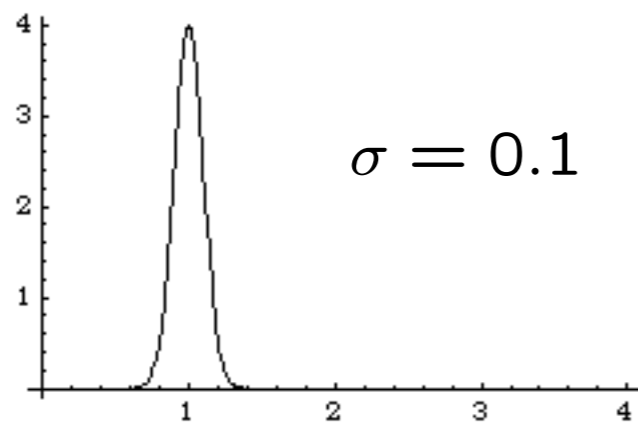
# Effect of Gaussian thickness variation

$$P(x) = \frac{1}{\sigma\sqrt{(2\pi)}} \exp\left(\frac{-(x - \bar{x})^2}{2\sigma^2}\right)$$

$P(x)$

$\mu x_{\text{eff}}$  and  $\mu \bar{x}$  vs  $\mu$

$\mu x_{\text{eff}}'$  vs  $\mu$

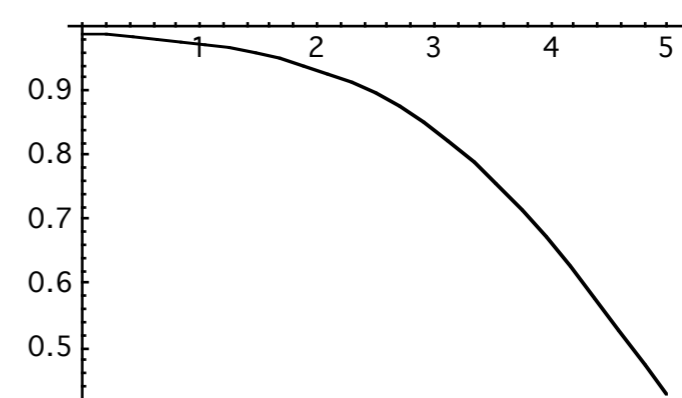
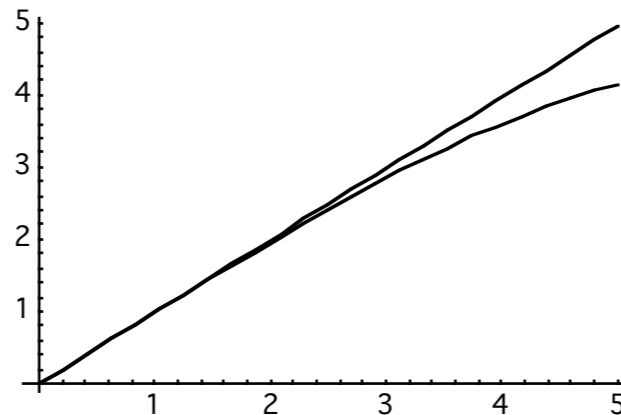
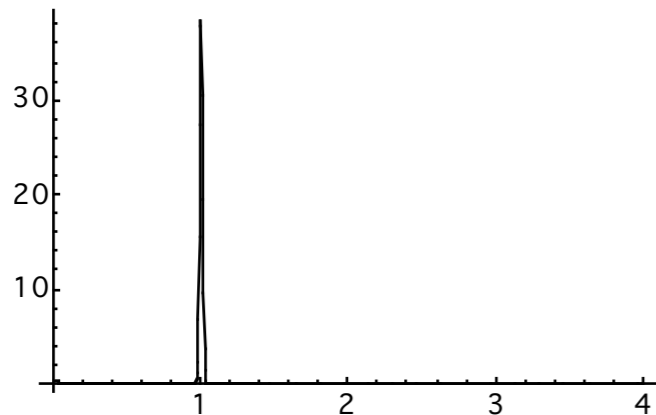


# Effect of leakage/harmonics

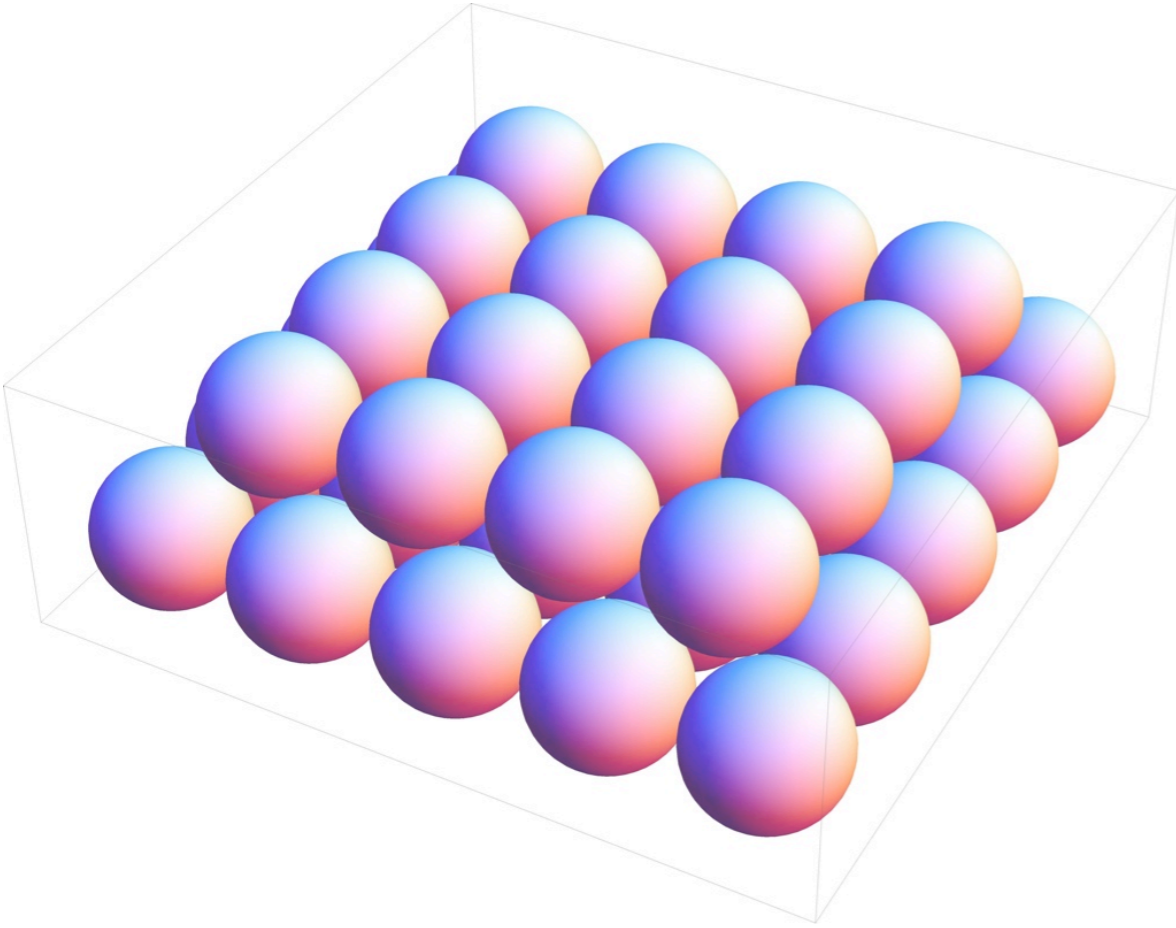
Leakage (zero thickness) fraction  $a$ , together with gaussian variation in thickness centered on  $x_0$  with width  $\sigma$ :

$$P(x) = a\delta(x) + (1 - a)\frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{(x - \bar{x})^2}{2\sigma^2}\right)$$

$$\mu x_{\text{eff}}(E) = -\ln(a + (1 - a)\exp(-\mu x_0 + \mu^2\sigma^2/2))$$

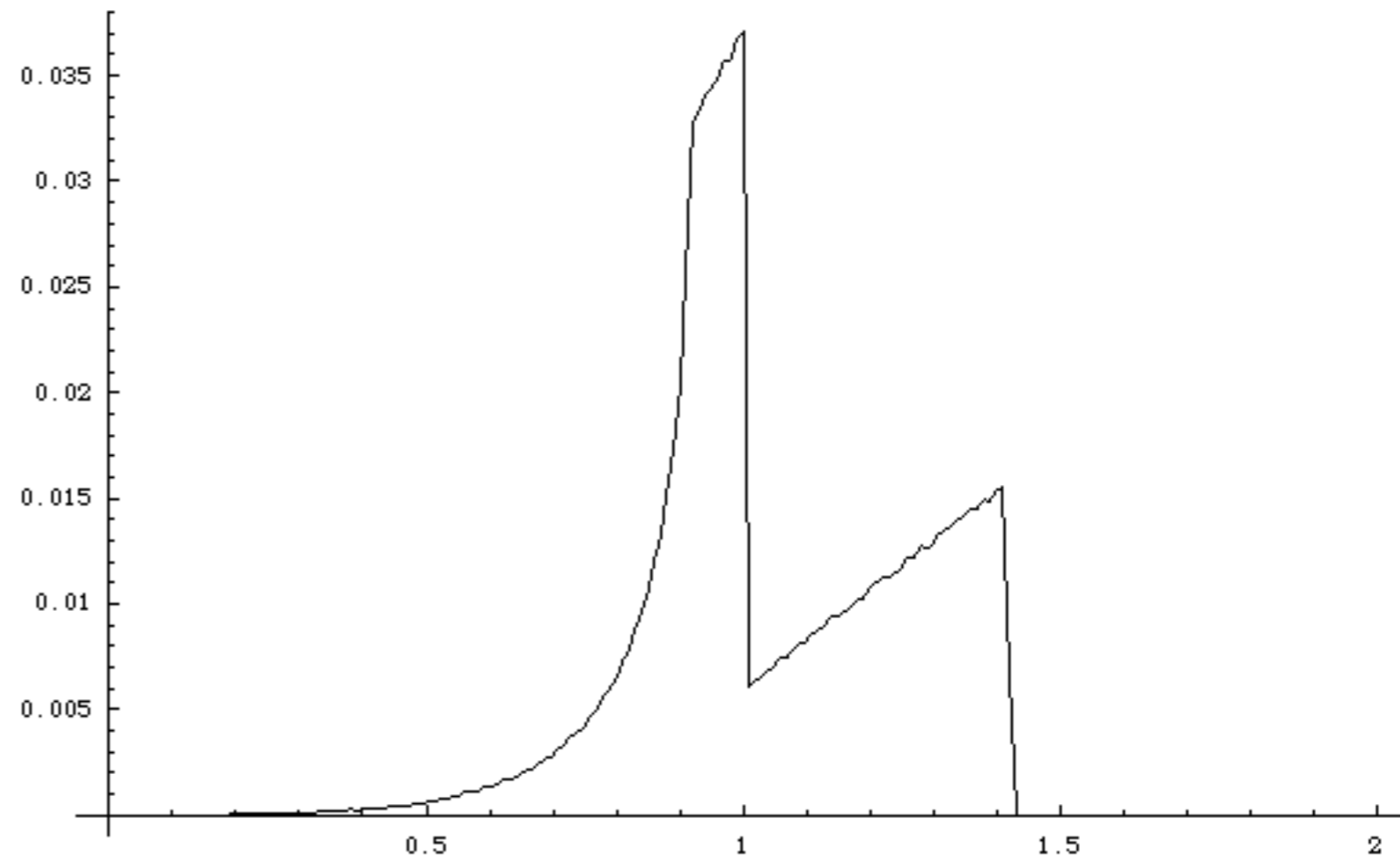


# Example - Layers of spheres



Layers of spheres  
stacked (no holes)

Thickness  
Distribution  
is broad



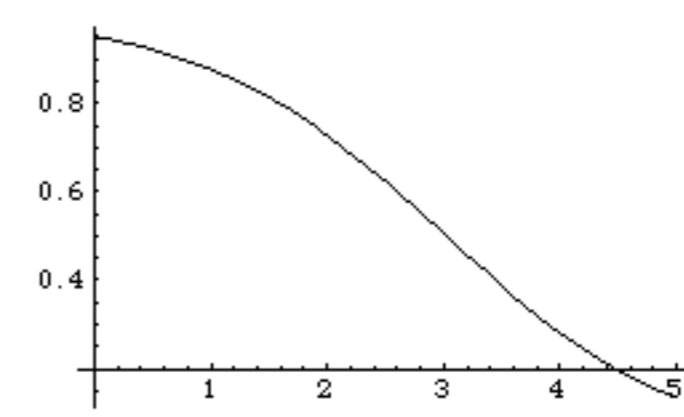
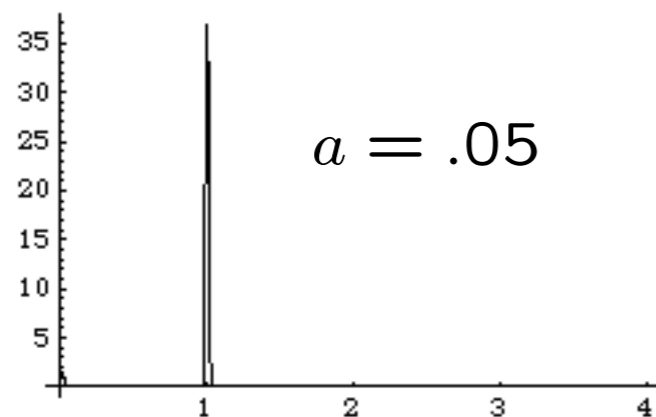
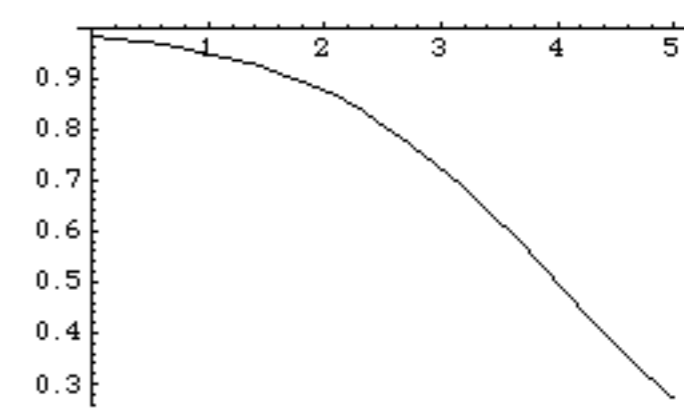
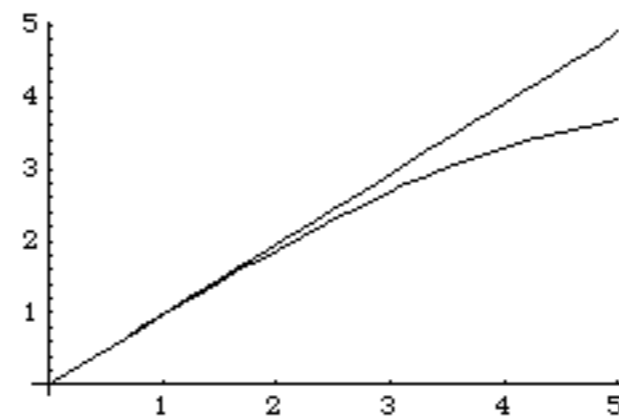
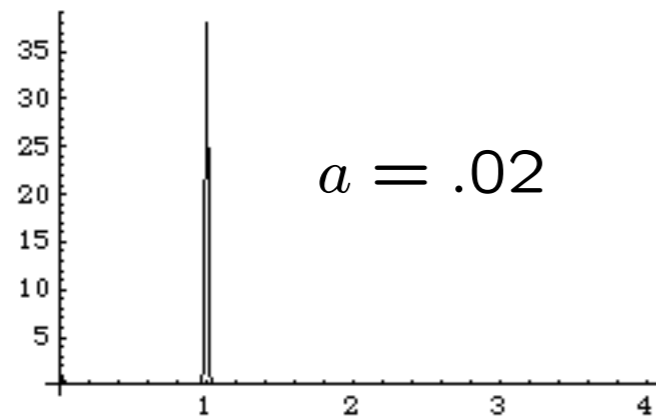
# Effect of pinholes (leakage) or harmonics

$$P(x) = a\delta(x) + (1 - a)\frac{1}{\sigma\sqrt{2\pi}} \exp\left(\frac{-(x - \bar{x})^2}{2\sigma^2}\right)$$

$P(x)$

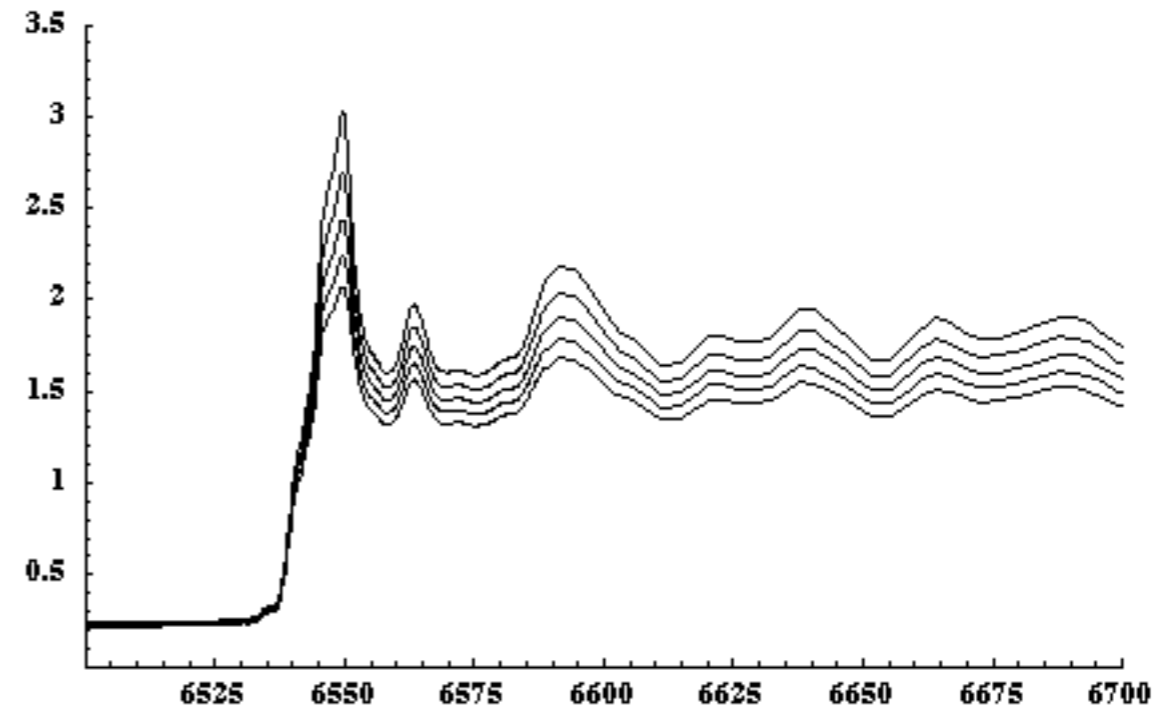
$\mu x_{\text{eff}}$  and  $\mu \bar{x}$  vs  $\mu$

$\mu x_{\text{eff}}'$  vs  $\mu$



# Effect of Leakage on spectra

- MnO 10 micron thick
- ~2 absorption lengths
- leakage varied from 0% to 10%
- Edge jump is reduced
- EXAFS amplitudes are reduced
- white line height compressed
- thickness effects distort both XANES and EXAFS - screw up fits and integrals of peak areas
- If you are fitting XANES spectra, watch out for these distortions



# Thickness effects always reduce EXAFS Amplitudes

The measured EXAFS is the variation in apparent absorption  $f(\mu)$  above the edge, divided by the measured edge step:

$$\chi_{\text{eff}} = \frac{f(\mu_a + \delta\mu) - f(\mu_a)}{f(\mu_a) - f(\mu_b)} \sim \frac{df}{d\mu} \Big|_{\mu_a} \frac{\delta\mu}{f(\mu_a) - f(\mu_b)}$$
 where  $\delta\mu$  is the true variation in  $\mu$  (which

us taken to be small), and  $\mu_a$  and  $\mu_b$  are respectively the absorption above and below the

edge. The true  $\chi$  is defined as  $\chi = \frac{(\mu_a + \delta\mu) - (\mu_a)}{\mu_a - \mu_b} = \frac{\delta\mu}{\mu_a - \mu_b}$ . Thus, thickness effects alter

the measured EXAFS amplitudes by the ratio:  $\frac{\chi_{\text{eff}}}{\chi} = \frac{df}{d\mu} \Big|_{\mu_a} \frac{\mu_a - \mu_b}{f(\mu_a) - f(\mu_b)}$ . To evaluate the right side of this equation, consider the Taylor expansion:

$$f(\mu_b) = f(\mu_a) + \frac{df}{d\mu} \Big|_{\mu_a} (\mu_b - \mu_a) + \frac{1}{2} \frac{d^2f}{d\mu^2} \Big|_{\mu_a} (\mu_b - \mu_a)^2 + \dots$$

This can be rewritten:

$$\frac{df}{d\mu} \Big|_{\mu_a} - \frac{f(\mu_a) - f(\mu_b)}{(\mu_a - \mu_b)} = \frac{1}{2} \frac{d^2f}{d\mu^2} \Big|_{\mu_a} (\mu_a - \mu_b) + \dots$$

The series is essentially an expansion in powers of a parameter of size roughly  $\sim \mu_a \sigma$ , where  $\sigma$  is the rms width of  $P(x)$ . From the previous discussion, the curvature of  $f$  is always negative or zero, and  $\mu_a > \mu_b$ , which implies that right side is negative or zero.

Therefore  $\chi_{\text{eff}} / \chi$  is less than (or at most equal to) unity.

[http://gbxafs.iit.edu/training/thickness\\_effects.pdf](http://gbxafs.iit.edu/training/thickness_effects.pdf)



# Simple model of thickness distribution

Thickness distribution is a sum of gaussians of weight  $a_n$ , thickness  $x_n$ , and width  $\sigma_n$ :

$$P(x) = \sum_n \frac{a_n}{\sigma_n \sqrt{2\pi}} \exp\left(-\frac{(x - x_n)^2}{2\sigma_n^2}\right)$$

$$\mu x_{\text{eff}}(E) = -\ln\left(\sum_n a_n \exp\left(-\mu x_n + \mu^2 \sigma_n^2 / 2\right)\right)$$

This expression can be used to estimate the effect of thickness variations

# Transmission -Summary

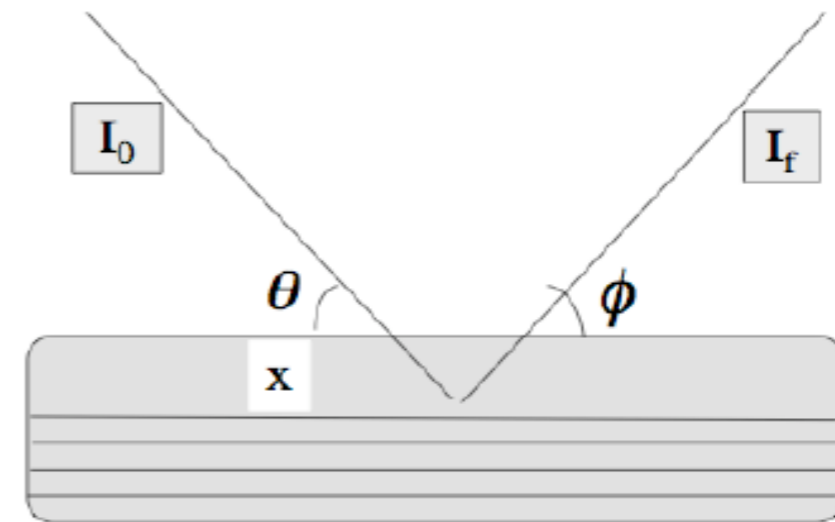
- Samples should be made uniform on a scale determined by the absorption length of the material
- Absorption length should be calculated when you're designing experiments and preparing samples

# When to choose Transmission

- You need to get x-rays through the sample
  - Total thickness should be kept below  $<2-3$  absorption lengths including substrates to minimize thickness effects
    - “beam hardening” - choose fill-gases of back ion chamber to minimize absorption of harmonics; get rid of harmonics by monochromator detuning, harmonic rejection mirrors, etc.
  - Element of interest must be concentrated enough to get a decent edge jump ( $> 0.1$  absorption length)
  - Pinholes and large thickness variations should be minimized
  - If you can't make a good transmission sample, consider using fluorescence or electron yield

# Fluorescence Radiation in the Homogeneous Slab Model

- Probability the photon penetrates to a depth  $x$  in the sample
- and that is absorbed by the element  $i$  in a layer of thickness  $dx$
- and as a consequence it emits with probability  $\epsilon$  a fluorescence photon of energy  $E_f$
- which escapes the sample and is radiated into the detector



- Thin Sample

$$dI_f = I_0 \epsilon_a \frac{\mu_a(E)}{\sin \theta} e^{-\frac{\mu(E)x}{\sin \theta}} e^{-\frac{\mu(E_f)x}{\sin \phi}} dx$$

$$I_f = \frac{I_0 \epsilon_a \left( \frac{\mu_a}{\sin \theta} \right)}{\frac{\mu_T}{\sin \theta} + \frac{\mu_f}{\sin \phi}} \left[ 1 - e^{-\left( \frac{\mu_T}{\sin \theta} + \frac{\mu_f}{\sin \phi} \right) d} \right]$$

$$\left[ \left( \frac{\mu_T}{\sin \theta} + \frac{\mu_f}{\sin \phi} \right) d \right] \ll 1$$

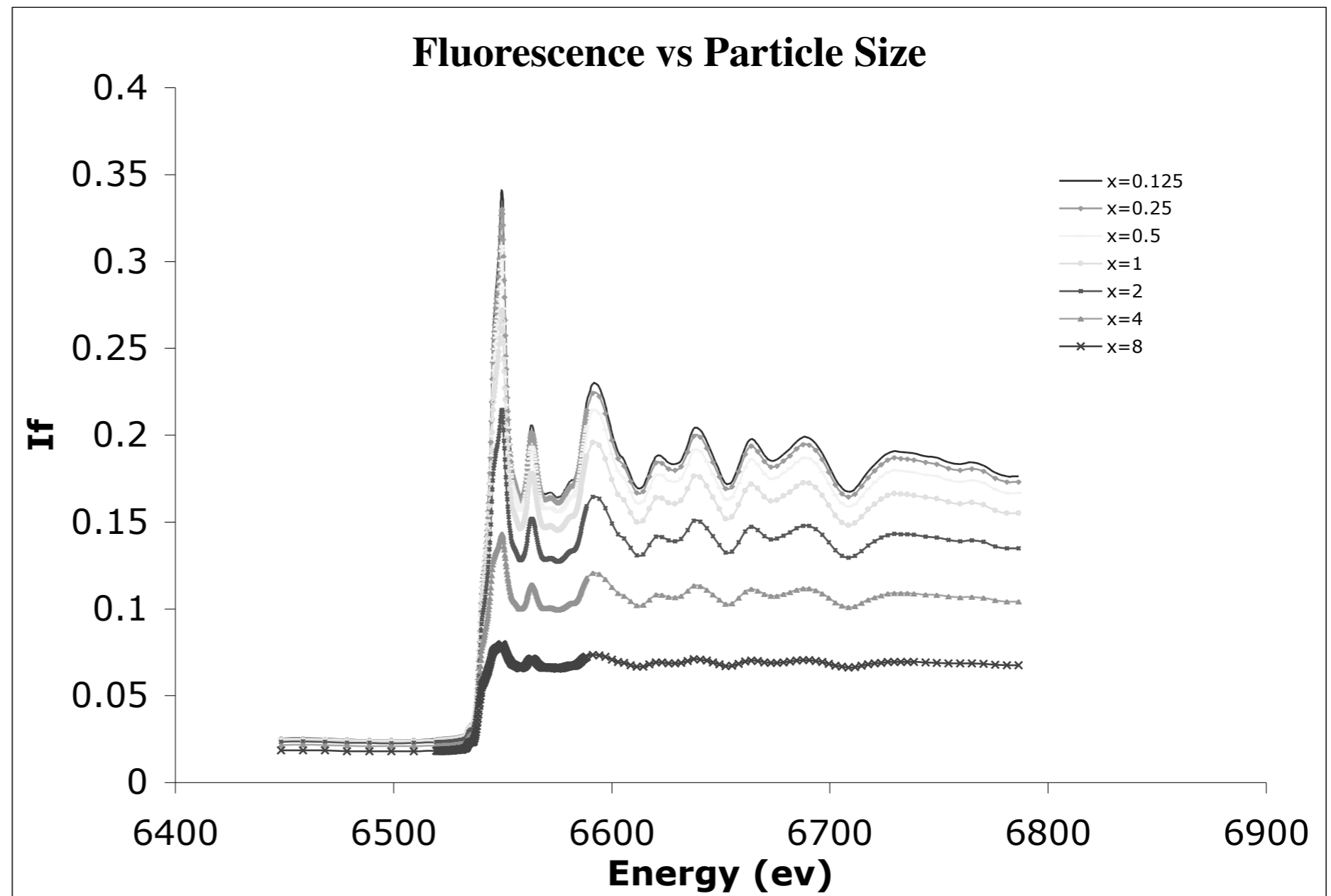
$$(I_f)_{thin} = I_0 \epsilon_a \left( \frac{\mu_a}{\sin \theta} \right) d$$

# Fluorescence samples

- Thin concentrated limit is simple
- Thick dilute limit is simple
- Thick concentrated requires numerical corrections (e.g. Booth and Bridges, Haskel's fluo). Thickness effects can be corrected also if necessary by regularization (Babanov et al).
- Sample Requirements
  - Particle size must be small compared to absorption lengths of particles (not just sample average)
    - Can be troublesome for in situ studies
  - Homogeneous distribution
  - Flat sample surface preferred

# Speciation problems

Nonlinear distortions of the spectra depend on particle size and distribution. This affects speciation results



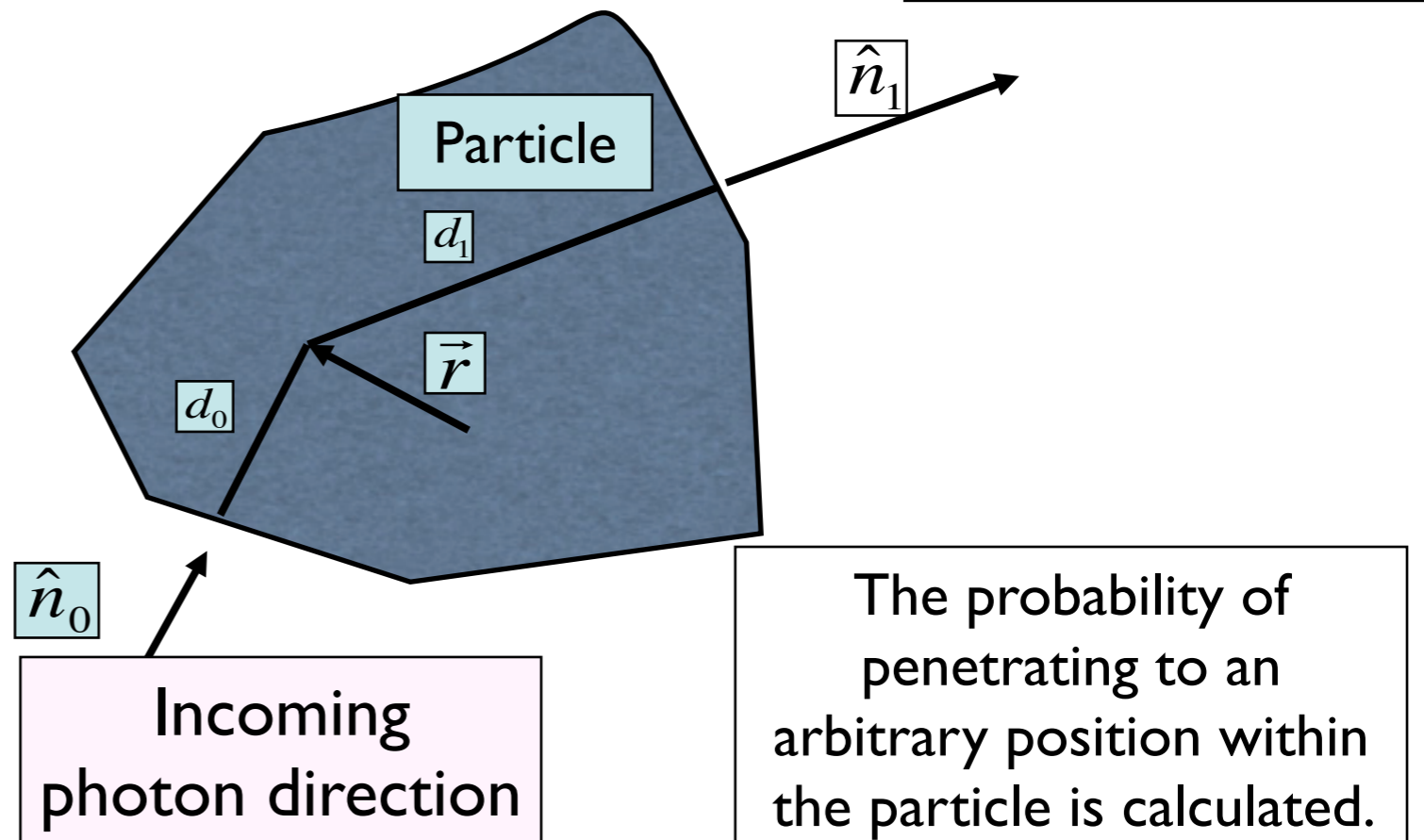
# Modeling Fluorescence

- Monte Carlo and analytical calculations of Tannazi and Bunker
- Analytical calculations build on work by Hunter and Rhodes, and Berry, Furuta and Rhodes (1972)

$$\hat{n}_0 = \sin \theta_0 \cos \phi_0 \hat{i} + \sin \theta_0 \sin \phi_0 \hat{j} + \cos \theta_0 \hat{k},$$

$$\hat{n}_1 = \sin \theta_1 \cos \phi_1 \hat{i} + \sin \theta_1 \sin \phi_1 \hat{j} + \cos \theta_1 \hat{k}$$

$$P_{\vec{r}} \propto e^{-\mu d_0} e^{-\mu_f d_1},$$



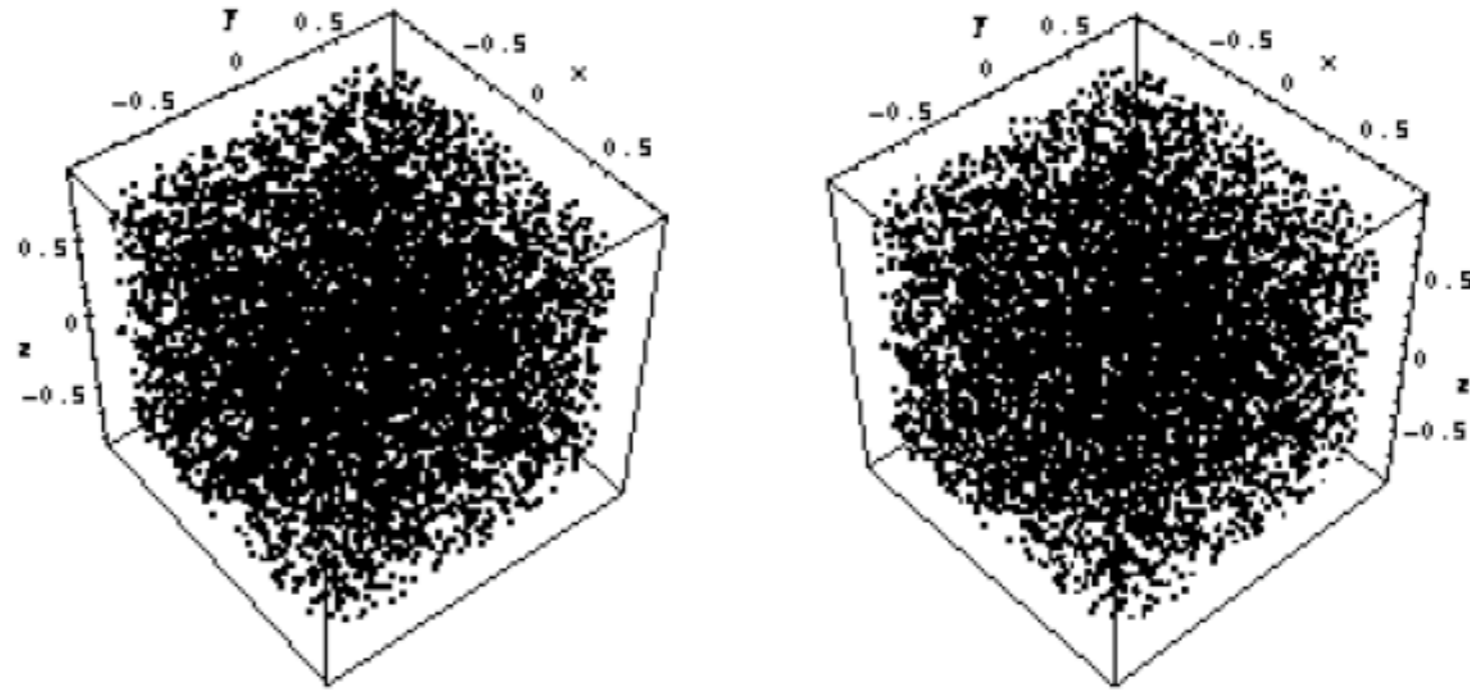
The probability of penetrating to an arbitrary position within the particle is calculated. This probability is averaged over the whole particle by Monte Carlo integration.

$$\bar{P} = \frac{P_{\vec{r}_1} + P_{\vec{r}_2} + \cdots + P_{\vec{r}_k}}{k}$$

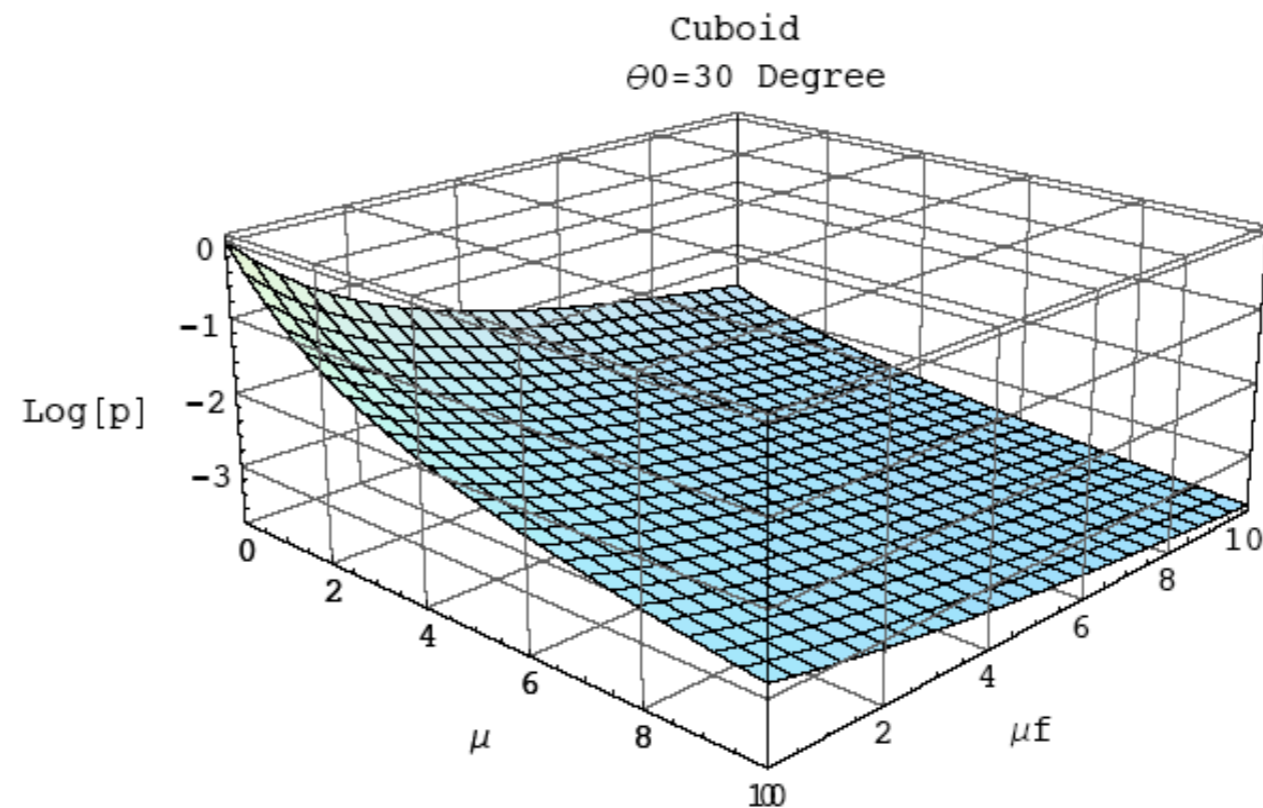
*Number of the points that satisfy the surface equation*



# Cuboidal Particles (stereo)

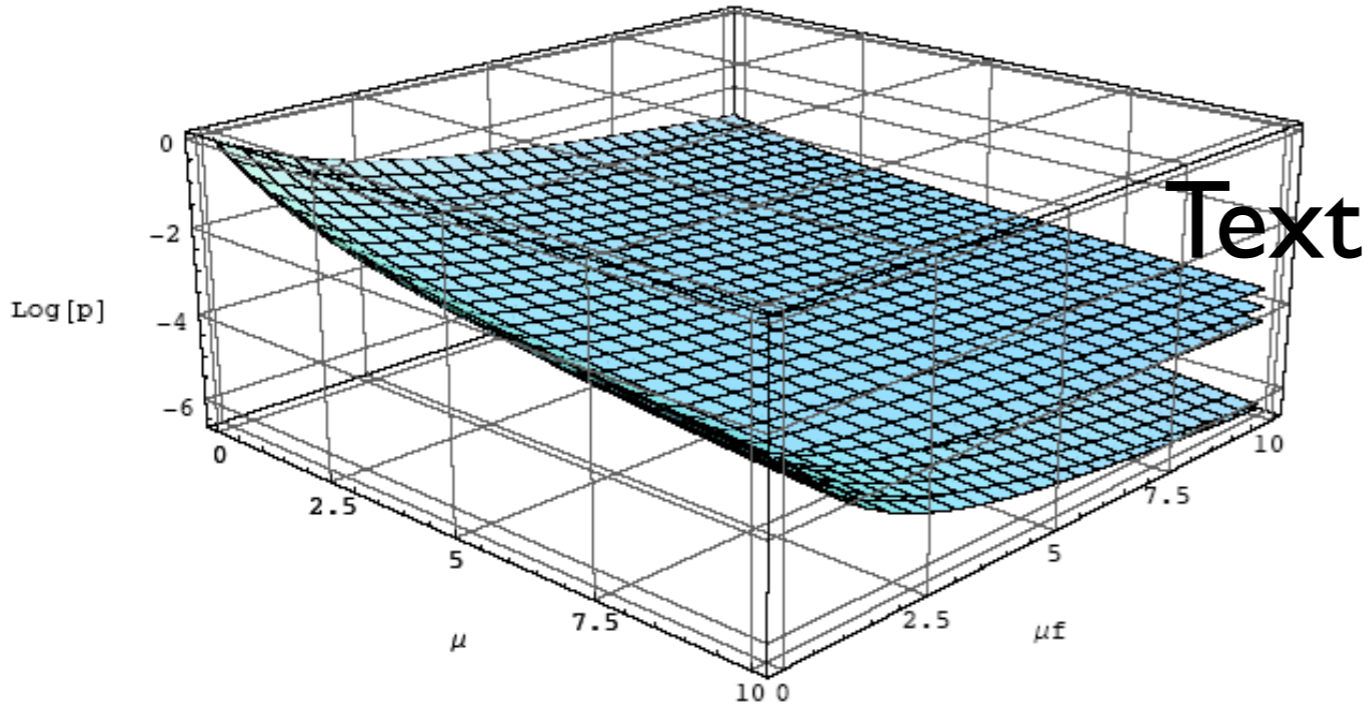


Calculate the  
probability  
as function  
of  $\mu$  and  $\mu_f$



# Different Orientations

$d_0, d_1$  maps  $\longrightarrow$



Even the particle orientation matters if particles too large

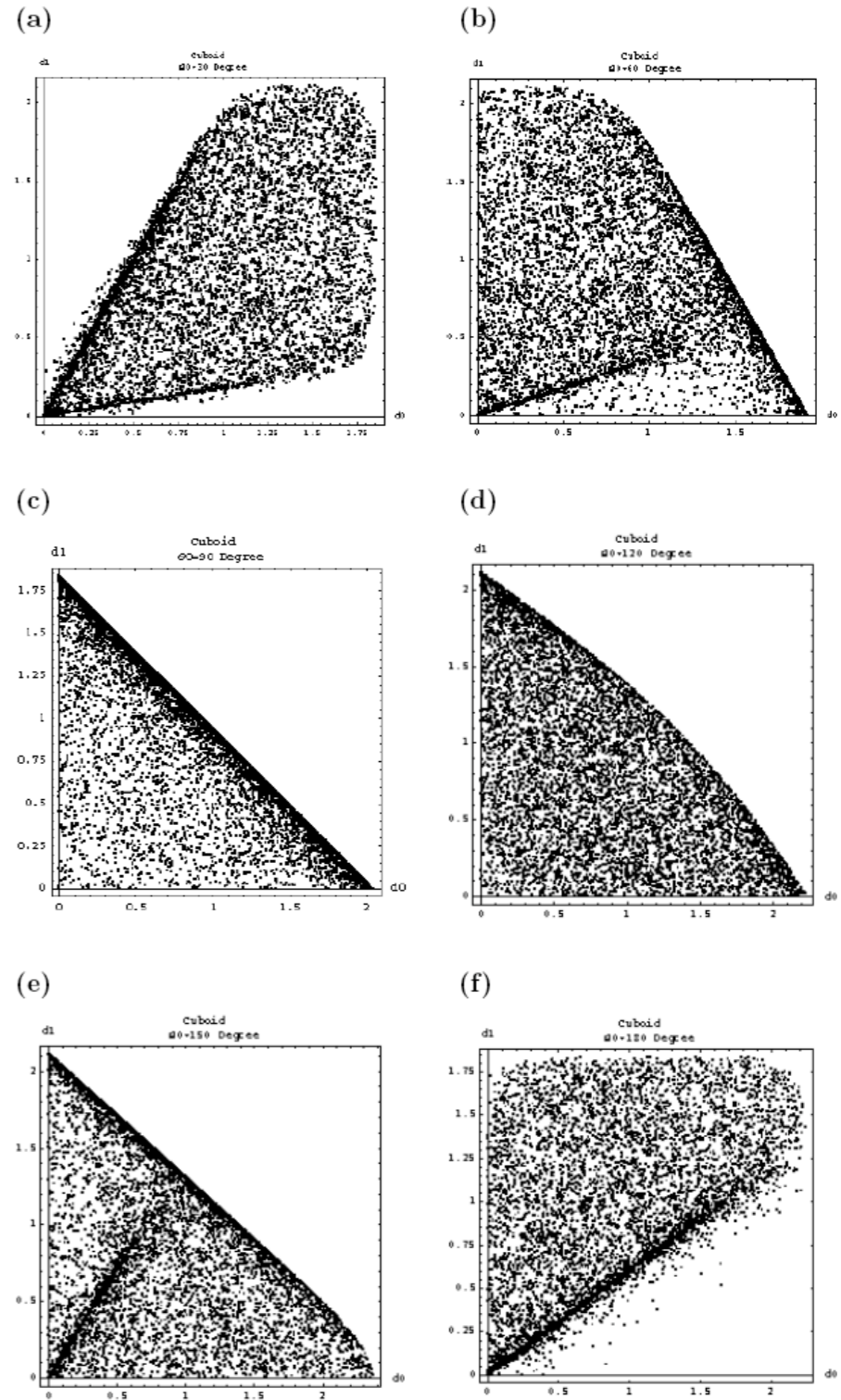
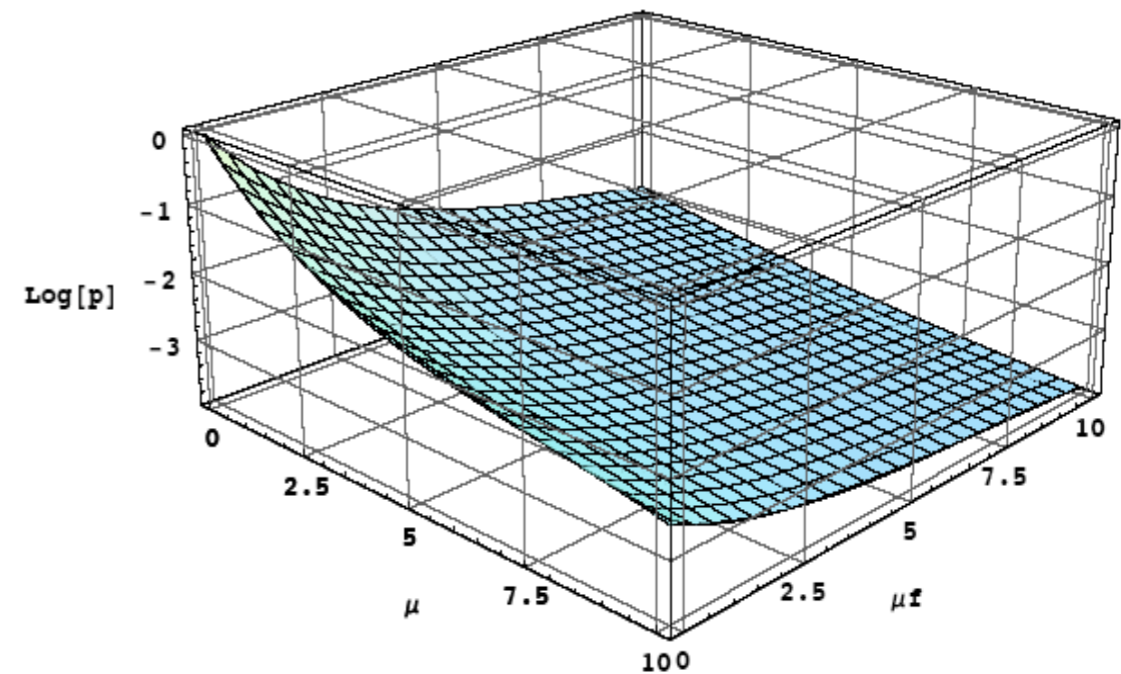


Figure 5.8.  $\{d_0, d_1\}$  Maps for Cuboid at  $\theta_0 =$ : (a) 30, (b) 60, (c) 90, (d) 120, (e) 150, and (f) 180 degrees and  $\theta_1 = \pi - \theta_0$  degrees.

$$\bar{P} = \int F(d_0, d_1) e^{-(\mu d_0 + \mu_f d_1)} dd_0 dd_1.$$

$$\log \bar{P} = \sum_{n=1}^{\infty} \sum_{m=1}^{\infty} \frac{(\mu)^n (\mu_f)^m}{n! m!} C_{nm}$$



- The log of the mean probability can be expanded as a power series in both  $\mu$  and  $\mu_f$ . The coefficients are related to the cumulants of the (2D) distribution of distances  $d_0, d_1$ . The main point is that the probabilities for a given shape of particle (and theta, phi) can be parameterized by a handful of numbers, the coefficients.

# Other shapes tabulated in Firouzeh Tannazi dissertation

easily calculated  
for any convex  
particle shape

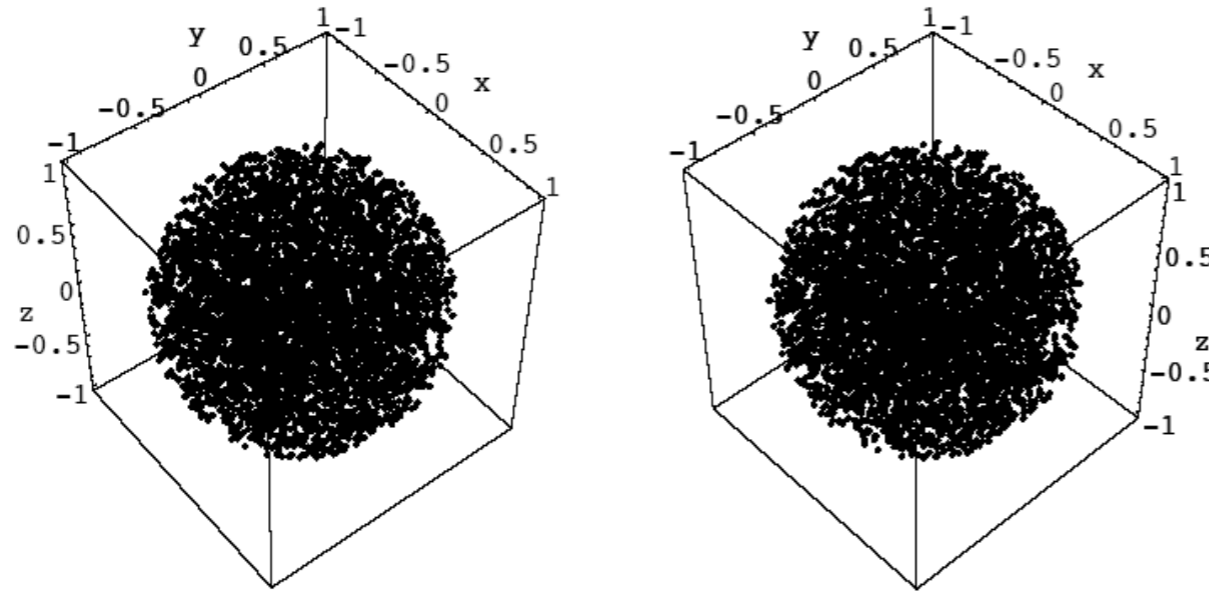


Figure 5.11. Sphere

Table 5.3. Cumulant Coefficients Table for Sphere

<i>Coeff.</i>	$\theta_0 = 30^\circ$	$\theta_0 = 60^\circ$	$\theta_0 = 90^\circ$	$\theta_0 = 120^\circ$	$\theta_0 = 150^\circ$	$\theta_0 = 180^\circ$
1	-0.0509	-0.051	-0.051	-0.0499	-0.0492	-0.0501
$\mu$	-0.6484	-0.651	-0.645	-0.6552	-0.6624	-0.6572
$\mu^2$	0.068	0.0677	0.0673	0.06798	0.0687	0.0683
$\mu^3$	-0.0029	-0.003	-0.0029	-0.0029	-0.0029	-0.0029
$\mu\mu_f$	0.13399	0.017	-0.1328	-0.1407	0.0033	0.12685
$\mu^2\mu_f$	-0.0158	0.0011	0.0173	0.0187	0.0034	-0.01459
$\mu^3\mu_f$	0.0007	-0.0001	-0.0008	-0.0008	-0.00023	0.00062
$\mu\mu_f^2$	-0.016	0.0018	0.0168	0.01783	0.0029	-0.01451
$\mu^2\mu_f^2$	0.0019	-0.0006	-0.0019	-0.00202	-0.00076	0.0017
$\mu^3\mu_f^2$	-0.00008	0.00004	0.00008	0.00008	0.00004	-0.000074
$\mu\mu_f^3$	0.00068	-0.00017	-0.00074	-0.00078	-0.00021	0.00062
$\mu^2\mu_f^3$	-0.00008	0.00004	0.00008	0.000081	0.00004	-0.00007
$\mu^3\mu_f^3$	$3.5 \times 10^{-6}$	$-2.1 \times 10^{-6}$	$-3.01 \times 10^{-6}$	$-3.08 \times 10^{-6}$	$-2.2 \times 10^{-6}$	$3.12 \times 10^{-6}$
$\mu_f$	-0.6521	-0.672	-0.6562	-0.6548	-0.663	-0.6468
$\mu_f^2$	0.0678	0.07063	0.0681	0.0683	0.0689	0.0663
$\mu_f^3$	-0.0029	-0.00301	-0.0029	-0.0029	-0.0029	-0.0028

# Dilution

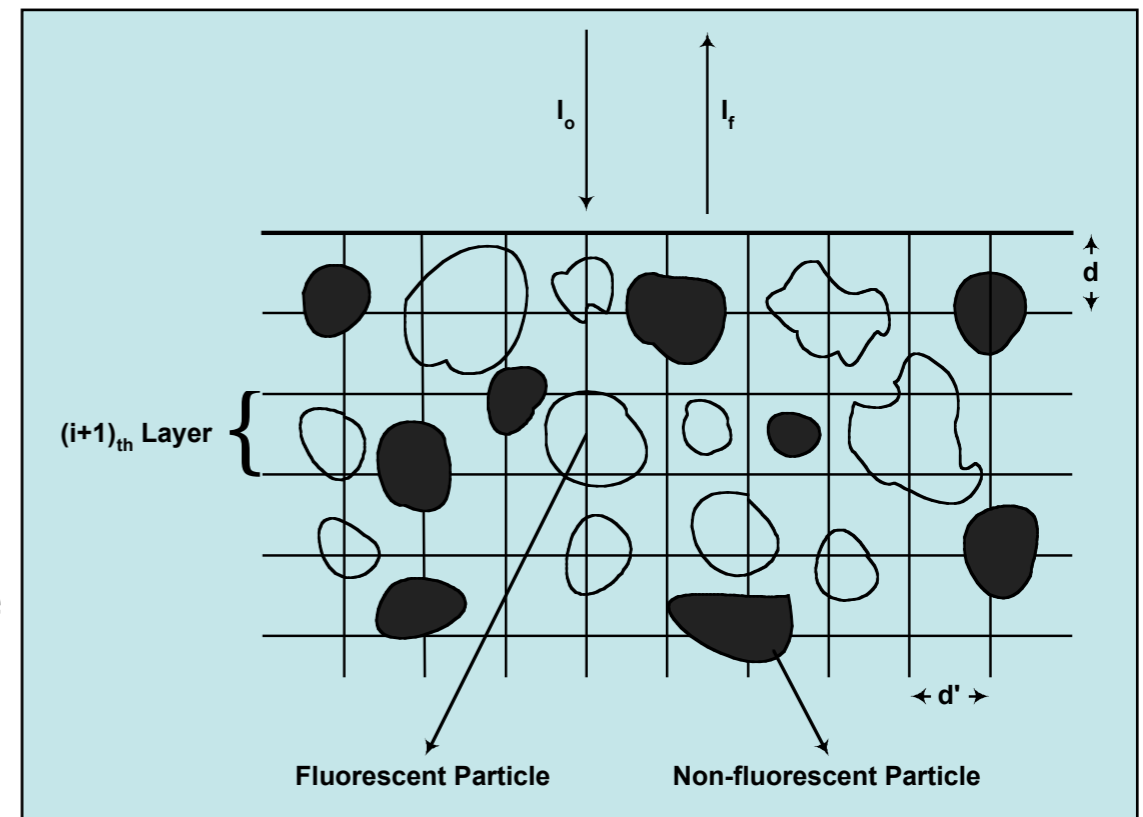
- Even if the sample is dilute on average you may not be really in the dilute limit
- Each fluorescent particle must be small enough, otherwise you will get distorted spectra
- Don't just mix up your particles with a filler and assume the sample is ok. Make the particles are small enough first, and calculate what "small" means.

# Hunter and Rhodes Model Continuous Size Distribution

- This model is a generalization of BFR model that has been developed by the authors above (1972), and is a formulation for continuous size distribution.
- In this approach we need to define a particle size distribution function:

$$\int_{a_{\min}}^{a_{\max}} f(a) da = 1$$

- Where  $a_{\min}$  and  $a_{\max}$  are the smallest and largest particle size in the sample and  $a$  is the particle size that is a variable in this approach.
- The probabilities term compare to the BFR model are defined as differential probabilities here:  $P_f(a, a') da$ .
- For calculation average transmission or fluorescence radiation through  $l$  layers we need to consider three different cases: No overlap in all layers, Some overlap and, total overlap.
- The total Fluorescence radiation is obtained from this formula, which we are adapting to XAFS.



## *HR Model*

$$dI(a)_{i+1} = \frac{I_0}{A} \cdot \bar{J}_i(a) \cdot \bar{J}_{if}(a) \cdot (dn_f(a))_a \cdot \bar{\alpha} \cdot F(a)$$

$$dI_f(a) = \frac{I_0 \epsilon_a \mu_a(E) \eta C_f f(a) [1 - e^{-\sqrt{2}(\mu_{Tf}(E) + \mu_f(E_f))a}]}{[\mu_{Tf}(E) + \mu_f(E_f)]} \times$$

$$\sum_{i=0}^n (\bar{J}(a) \cdot \bar{J}(a))^i$$

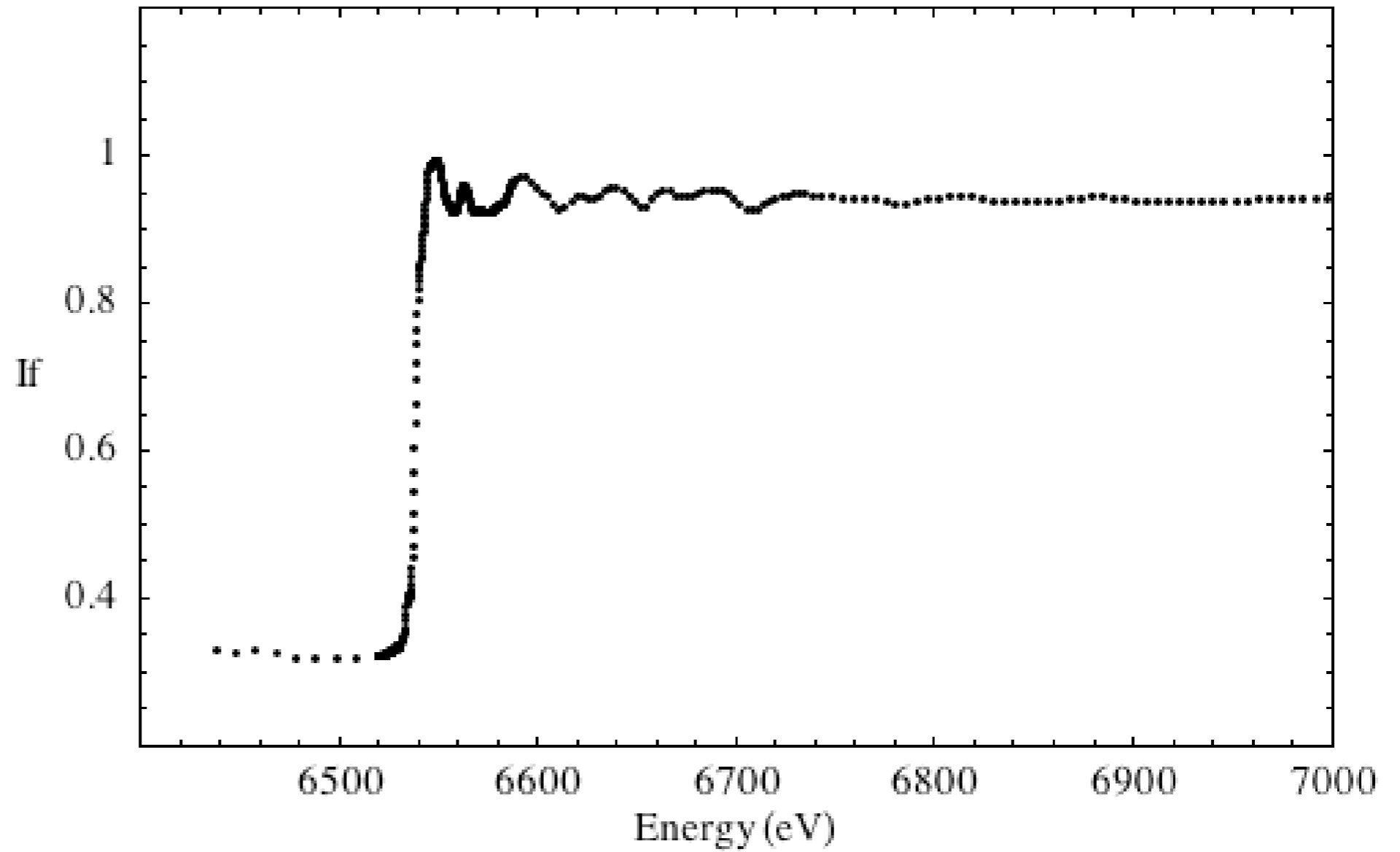
$$J_1(a) = 1 - a\eta \int_{a_{\min}}^{a_{\max}} \frac{1}{\bar{d}} (C_f f(a') [1 - e^{-\sqrt{2}\mu_{Tf}(E)\bar{d}}] +$$

$$C_n g(a') [1 - e^{-\sqrt{2}\mu_{Tn}(E)\bar{d}}]) da'$$

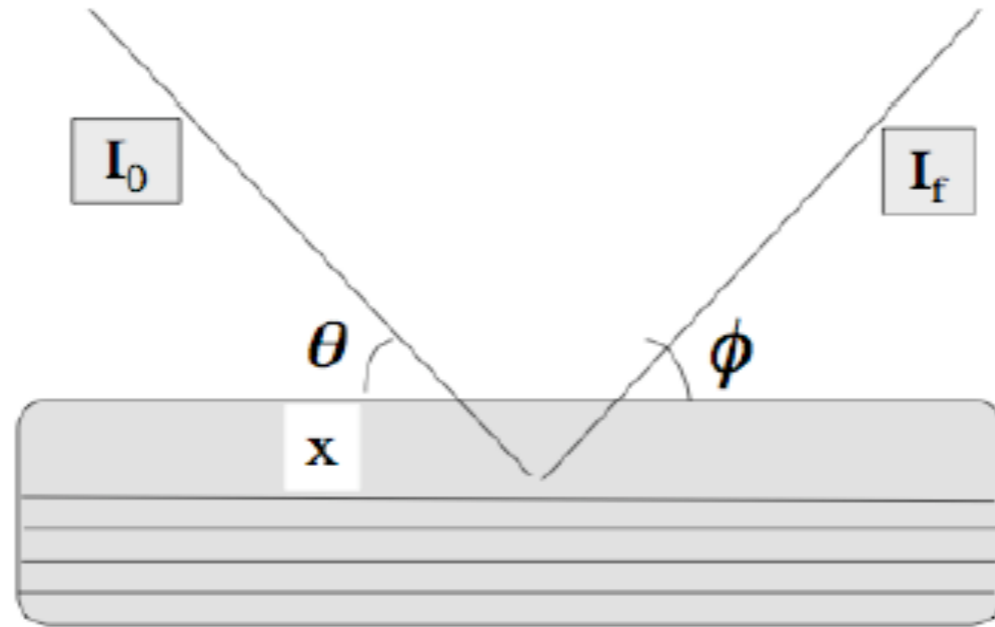
# *HR Model*

nonlinear  
compression  
of spectra

Fluorescence in HR Model



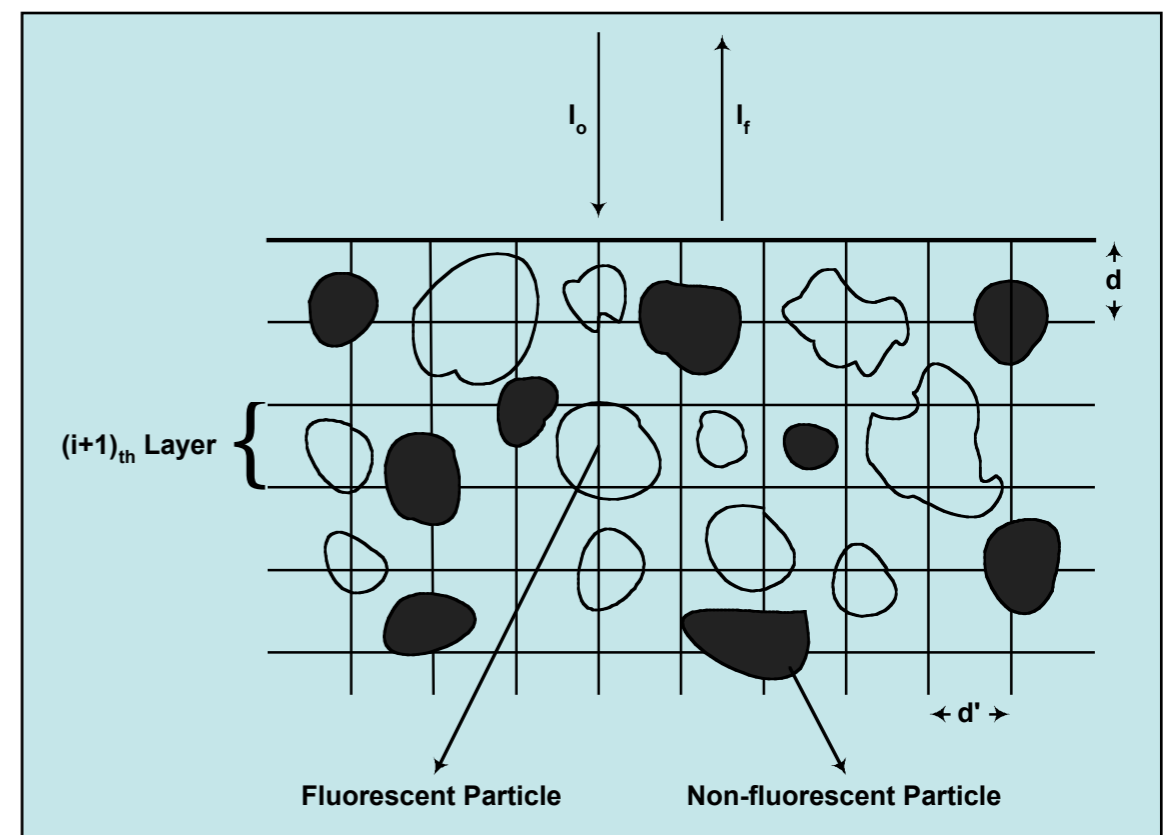
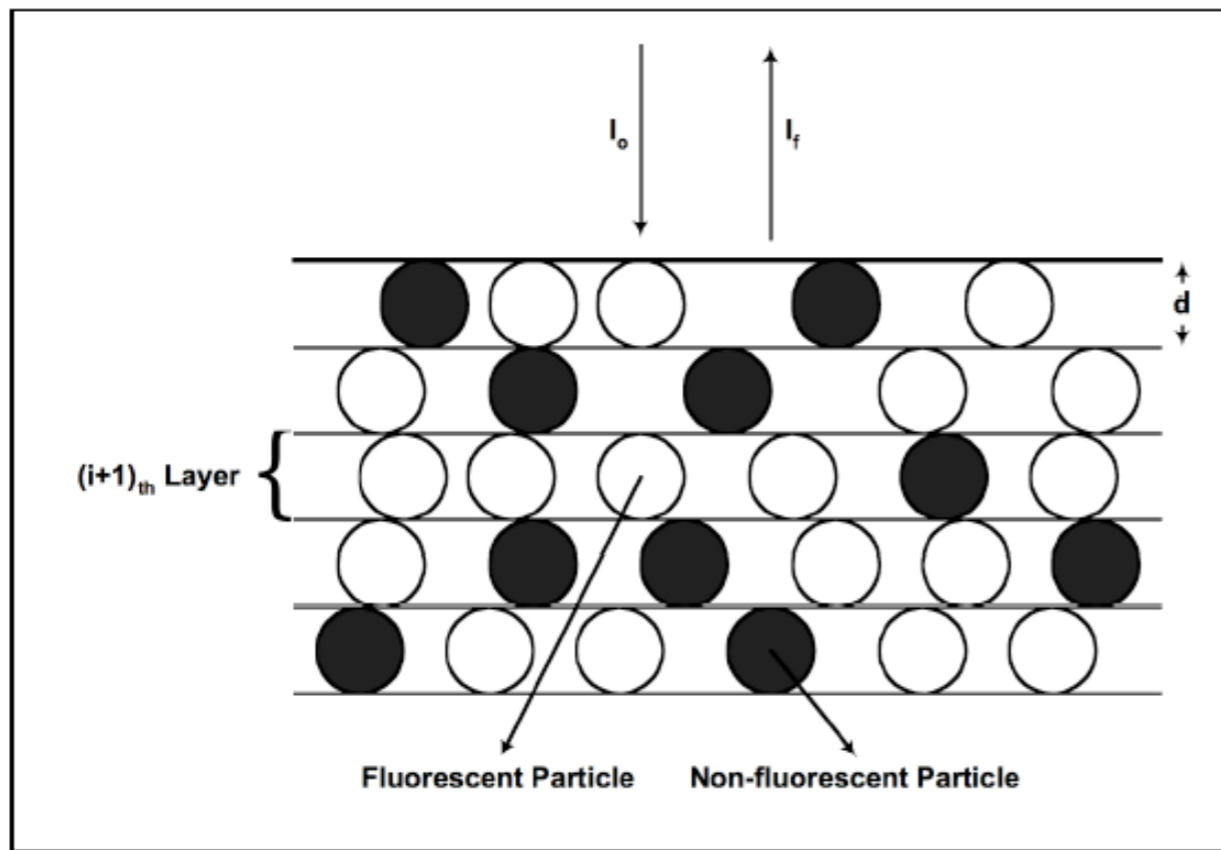




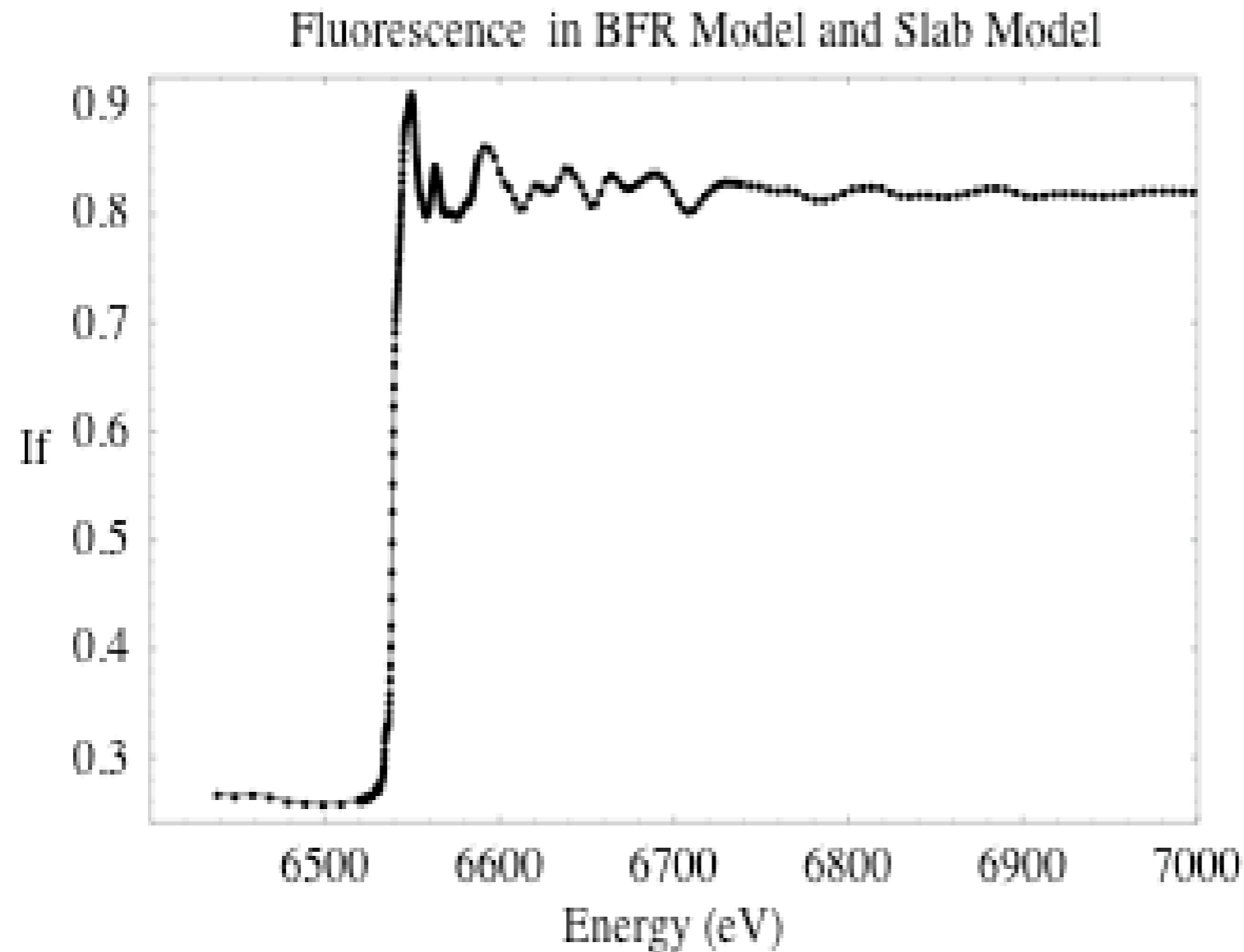
$$\eta \rightarrow 1$$

$$C_f \rightarrow 1$$

$$f(x) = \delta(x - a)$$



# Comparison between BFR, HR, and Slab Model



All 3 models agree in the appropriate limits

# Summary - Fluorescence

- Particle size effects are important in fluorescence as well as transmission
- The homogeneous slab model is not always suitable but other models have been developed
- If the particles are not sufficiently small, their shape, orientation, and distribution can affect the spectra in ways that can influence results
- Particularly important for XANES and speciation fitting

# Electron yield detection

- sample placed atop and electrically connected to cathode of helium filled ion chamber
- electrons ejected from surface of sample ionize helium - their number is proportional to absorption coefficient
- The current is collected as the signal just like an ionization chamber
- Surface sensitivity of electron detection eliminates self-absorption problems but does not probe the bulk material

# Sample Inhomogeneities

- Importance of inhomogeneity also can depend on spatial structure in beam
  - bend magnets and wiggler beams usually fairly homogeneous
- Undulator beams trickier because beam partially coherent
  - coherence effects can result in spatial microstructure in beam at micron scales
- Beam Stability
- Samples must not have spatial structure on the same length scales as x-ray beam. Change the sample, or change the beam.

- Foils and films often make good transmission samples
  - stack multiple films if possible to minimize through holes
    - check for thickness effects (rotate sample)
- Foils and films can make good thin concentrated or thick dilute samples in fluorescence
- Consider grazing incidence fluorescence to reduce background and enhance surface sensitivity

# Solutions

- Usually solutions are naturally homogeneous
  - Can make good transmission samples if concentrated
  - Usually make good fluorescence samples ( $\sim 1$  millimolar and 100 ppm are routine), lower concentrations feasible
- They can become inhomogeneous during experiment
  - phase separation
  - radiation damage can cause precipitation (e.g. protein solutions)
  - photolysis of water makes holes in intense beams
  - suspensions/pastes can be inhomogeneous

# Particulate samples

- First calculate the absorption length for the material
- prepare particles that are considerably smaller than one absorption length of their material, at an energy above the edge
- Many materials require micron scale particles for accurate results
- Distribute the particles uniformly over the sample cross sectional area by dilution or coating



# Making Fine Particles

- During synthesis -> choose conditions to make small particles
- Grinding and separating
  - sample must not change during grinding (e.g. heating)
  - For XAFS can't use standard methods (e.g. heating in furnace and fluxing) from x-ray spectrometry, because chemical state matters
  - Have to prevent aggregation back into larger particles

# Grinding Materials

- Dilute samples - have to prevent contamination
- mortar and pestle (porcelain or agate (a form of quartz))
- inexpensive small volume ball mill (e.g. “wig-l-bug” ~\$700 US)
  - agate vials available
  - disposable plastic vials for mixing
  - standard for infrared spectrometry
- Frisch mill (several thousands of \$K US)  
e.g. MiniMill 2 Panalytical, Gilson Micromill



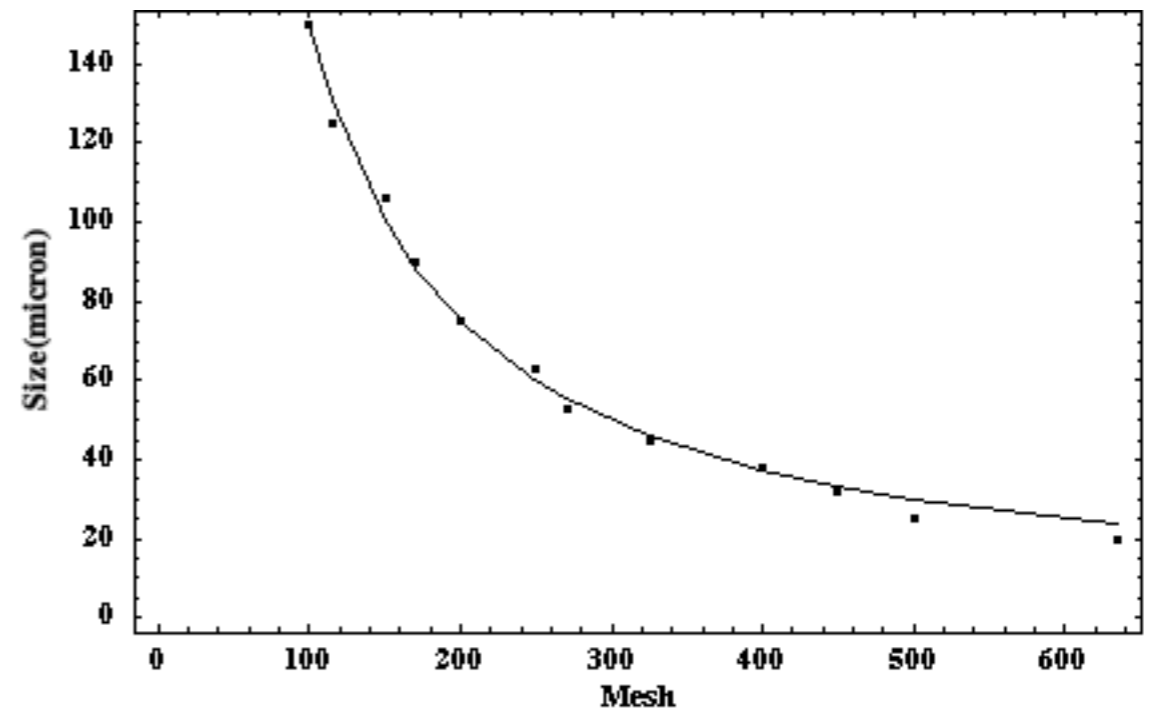
# Sieves

- 3" ASTM sieves work well
  - Screen out larger particles with coarse mesh (100 mesh)
  - pass along to next finer sieve
  - Sieve stack and shaker
- Usually can do well with 100, 200, 325, 400, 500, 635 mesh
- Still only guarantees 20 micron particles, too big for many samples



size (microns)  
~ 15000/mesh

100 mesh	150 $\mu\text{m}$
115 mesh	125 $\mu\text{m}$
150 mesh	106 $\mu\text{m}$
170 mesh	90 $\mu\text{m}$
200 mesh	75 $\mu\text{m}$
250 mesh	63 $\mu\text{m}$
270 mesh	53 $\mu\text{m}$
325 mesh	45 $\mu\text{m}$
400 mesh	38 $\mu\text{m}$
450 mesh	32 $\mu\text{m}$
500 mesh	25 $\mu\text{m}$
635 mesh	20 $\mu\text{m}$



# sedimentation

Selecting yet  
smaller  
particles

Drag force on a spherical particle of radius  $R$  moving at velocity  $v$  in fluid of viscosity  $\eta$ :  $F = 6\pi\eta Rv$ . Particles of density  $\rho$  will fall through the fluid of density  $\rho_0$  at a speed in which the particle's weight, less the buoyancy force, equals the drag force:

$$(\rho - \rho_0)\frac{4}{3}\pi R^3 g = 6\pi\eta Rv.$$

If the height of the fluid in the container is  $h$ , the time  $t$  that it would take all particles of radius  $R$  to fall to the bottom would then be:

$$t = \frac{9}{5} \frac{\eta h}{(\rho - \rho_0)gR^2}$$

# Sedimentation cont'd

- By knowing the densities of the material and the liquid (e.g. acetone), and the viscosity, the fluid height, and the required particle radius, you calculate the time.
- Mix it in, stir it up
  - wait the required time
  - decant the supernatant with a pipette
  - dry particles in a dish in a fume hood
- Must have non-reactive liquid

# worked example

Example: MnO in acetone at 20C

viscosity of acetone :

$$\eta = 0.0032 \text{ Poise}$$

$$= 0.0032 \text{ g}/(\text{cm} * \text{s})$$

$$R = 1\mu\text{m} = 3 * 10^{-4} \text{cm}$$

$$\text{density of acetone: } \rho_0 = 0.79 \frac{\text{g}}{\text{cm}^3}$$

$$\text{density of MnO: } \rho = 5.4 \frac{\text{g}}{\text{cm}^3}$$

$$h = 5\text{cm}$$

$$g = 980\text{cm}/\text{s}^2$$

$$\rightarrow t = 638 \text{ seconds.}$$

# Assembling Samples

- A) Mix uniformly (use wig-l-bug) into filler or binder
  - nonreactive, devoid of the element you are measuring, made of a not-too-absorbant substance e.g. Boron Nitride, polyvinyl alcohol, corn starch
  - Place into a sample cell (x-ray transparent windows e.g kapton or polypropylene), or press to make pellet
- B) Apply uniform coating to adhesive tape
  - Scotch Magic Transparent Tape (clean, low absorption)
  - use multiple layers to cover gaps between particles
  - watch for brush marks/striations
- C) Make a “paint” (e.g. Duco cement thinned with acetone)

# Checking the sample

- check composition by spectroscopy or diffraction
- visually check for homogeneity
  - caveat: x-ray vs optical absorption lengths
- tests at beamline: move and rotate sample
- digital microscope (Olympus Mic-D \$800 US)
- particle size analysis (Image/J free)
- If you have nice instruments like a scanning electron microscope or light scattering particle size analyzer, don't hesitate to use them



# Preferred Orientation

- If your sample is polycrystalline, it may orient in non-random way if applied to a substrate
- since the x-ray beams are polarized this can introduce an unexpected sample orientation dependence
- Test by changing sample orientation
- Magic-angle spinning to eliminate effect

# Control samples

- In fluorescence measurements always measure a blank sample without the element of interest under the same conditions as your real sample
- Many materials have elements in them that you wouldn't expect that can introduce spurious signals
- Most aluminum alloys have transition metals
- Watch out for impurities in adhesive films
- Fluorescence from sample environment excited by scattered x-rays and higher energy fluorescence

# HALO

- Harmonics
  - get rid of them
- Alignment
  - beam should only see uniform sample
- Linearity
  - detectors and electronics must linear
- Offsets
  - subtract dark currents regularly

# Conclusion

- Absorption coefficients increase dramatically at low energies  $\sim 1/E^3$ . Calculate the absorption coefficients so you know what you are dealing with at the energies you care about. Think like an x-ray. Know what to expect.
- Make particles much smaller than the absorption length above the edge, and ensure samples are homogeneous. Check experimentally for thickness, particle size, and self absorption effects
- Make sure materials within the sample are not reactive with sample cell or windows.